# Statistics

## 1 Linear combinations of random variables

### Continuous random variables

A continuous random variable X has a pdf f such that:

- 1.  $f(x) \ge 0 \forall x$
- $2. \int_{-\infty}^{\infty} f(x) dx = 1$

$$\Pr(X \le c) = \int_{-\infty}^{c} f(x) \, dx$$

Linear functions  $X \to aX + b$ 

$$\Pr(Y \le y) = \Pr(aX + b \le y)$$
$$= \Pr\left(X \le \frac{y - b}{a}\right)$$
$$= \int_{-\infty}^{\frac{y - b}{a}} f(x) dx$$

Mean:

$$E(aX + b) = a E(X) + b$$

Variance:

$$Var(aX + b) = a^2 Var(X)$$

Linear combination of two random variables

Mean:

$$E(aX + bY) = a E(X) + b E(Y)$$

Variance:

$$Var(aX + bY) = a^2 Var(X) + b^2 Var(Y)$$

(if X and Y are independent)

# 2 Sample mean

Approximation of the **population mean** determined experimentally.

$$\overline{x} = \frac{\Sigma x}{n}$$

where n is the size of the sample (number of sample points) and x is the value of a sample point

#### On CAS

- 1. Spreadsheet
- 2. In cell A1: mean(randNorm(sd, mean, sample size))
- 3. Edit  $\rightarrow$  Fill  $\rightarrow$  Fill Range
- 4. Input range as A1:An where n is the number of samples
- 5. Graph  $\rightarrow$  Histogram