

Statistics

1 Probability

$$\Pr(A \cup B) = \Pr(A) + \Pr(B) - \Pr(A \cap B)$$

$$\Pr(A \cup B) = 0 \quad (\text{mutually exclusive})$$

2 Conditional probability

$$\Pr(A|B) = \frac{\Pr(A \cap B)}{\Pr(B)} \quad \text{where } \Pr(B) \neq 0$$

$$\Pr(A) = \Pr(A|B) \cdot \Pr(B) + \Pr(A|B') \cdot \Pr(B') \quad (\text{law of total probability})$$

$$\Pr(A \cap B) = \Pr(A|B) \times \Pr(B) \quad (\text{multiplication theorem})$$

For independent events:

- $\Pr(A \cap B) = \Pr(A) \times \Pr(B)$
- $\Pr(A|B) = \Pr(A)$
- $\Pr(B|A) = \Pr(B)$

2.1 Discrete random distributions

Any experiment or activity involving chance will have a probability associated with each result or *outcome*. If the outcomes have a reference to **discrete numeric values** (outcomes that can be counted), and the result is unknown, then the activity is a *discrete random probability distribution*.

2.1.1 Discrete probability distributions

If an activity has outcomes whose probability values are all positive and less than one ($\implies 0 \leq p(x) \leq 1$), and for which the sum of all outcome probabilities is unity ($\implies \sum p(x) = 1$), then it is called a *probability distribution* or *probability mass function*.

- **Probability distribution graph** - a series of points on a cartesian axis representing results of outcomes. $\Pr(X = x)$ is on y -axis, x is on x axis.
- **Mean** μ - measure of central tendency. *Balance point* or *expected value* of a distribution. Centre of a symmetrical distribution.
- **Variance** σ^2 - measure of spread of data around the mean. Not the same magnitude as the original data. Represented by $\sigma^2 = \text{Var}(x) = \sum (x - \mu)^2 \times p(x) = \sum (x - \mu)^2 \times \Pr(X = x)$. Alternatively: $\sigma^2 = \text{Var}(X) = \sum x^2 \times p(x) - \mu^2$
- **Standard deviation** σ - measure of spread in the original magnitude of the data. Found by taking square root of the variance: $\sigma = \text{sd}(X) = \sqrt{\text{Var}(X)}$